

# Sunbelt XXVI

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## How to reveal the Informal Structure of Organizations.

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### Organizational Network Analysis

- Organizational research has increasingly been influenced by the network paradigm during the last years.
- Research focuses on topics like
  - social capital (on the individual or structural level)
  - the embeddedness of actors (individuals or organizations) in the economic system
  - relations between organizations (e.g. firm alliances)
  - knowledge management in organizations

Network analytical methods are increasingly applied in the consulting business.

### Organizational Design & Informal Structure

There are many organizational design factors, e.g.

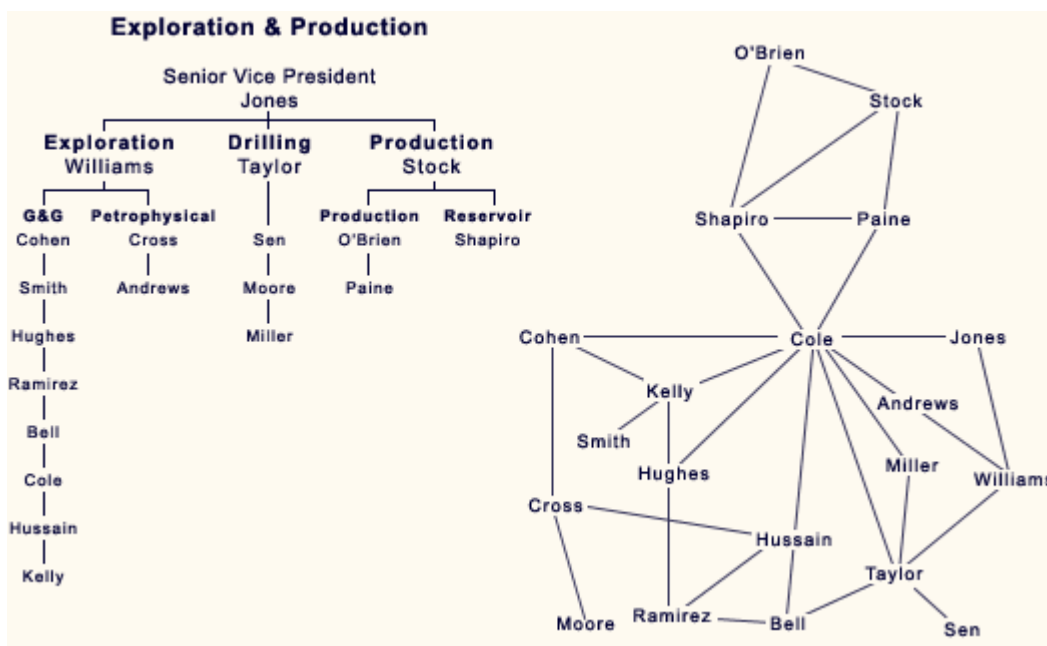
formal structure	arrangements
<ul style="list-style-type: none"><li>• org chart (functional structure)</li><li>• affiliation to teams</li><li>• workflow</li></ul>	<ul style="list-style-type: none"><li>• spatial arrangements</li><li>• temporal arrangements</li><li>• "span of control"</li></ul>

- On the other hand, the informal structure reflects the social relations between the members of an organization. These may be influenced by organizational design factors and/or by exogenous factors.
- A number of classical studies deal with the deviation of the informal structure of an organization from its formal structure.

### Where do we start from?

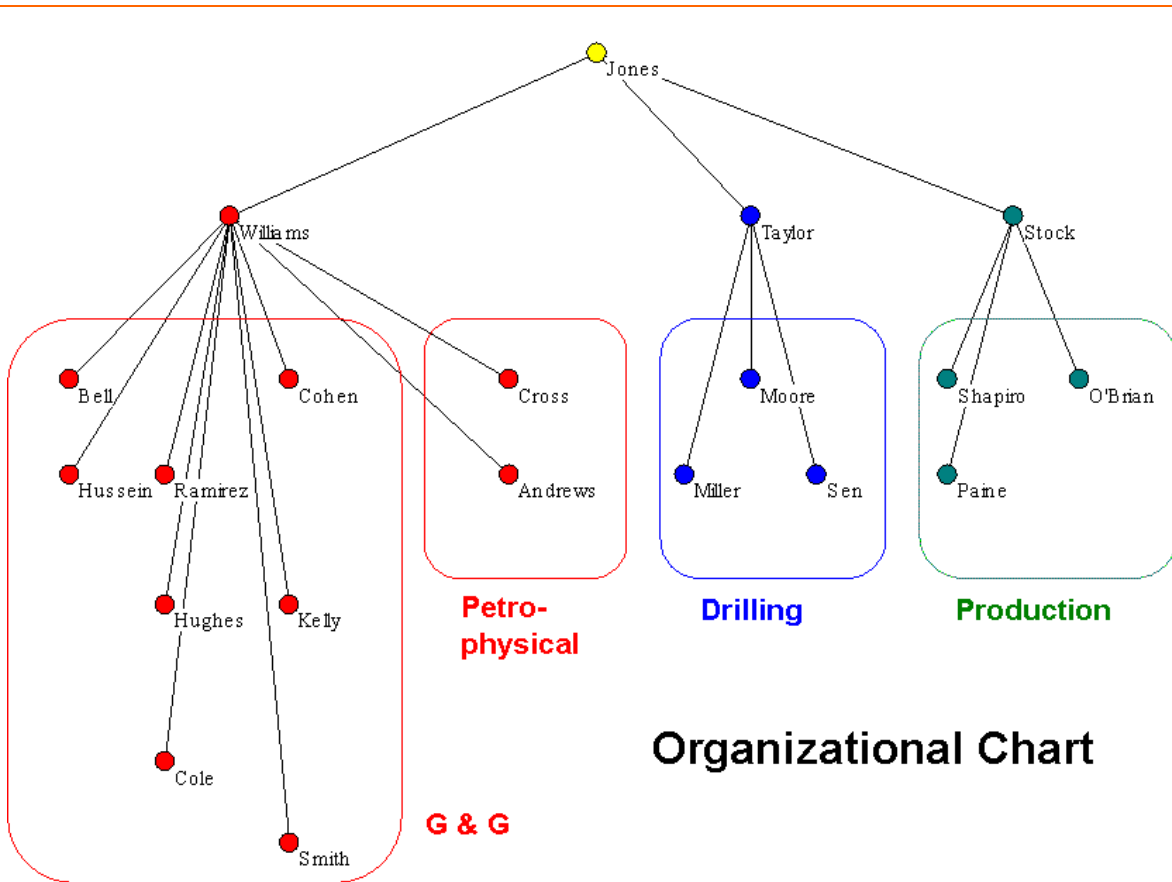
- Our objectives are
  - to contrast the design of an organization with its informal structure
  - to visualize and to measure the deviation of the informal structure from the organizational design
- Starting point is a **network-model of the organization** (e.g. the organizational chart).
  - the formal structure defines relations between the actors
  - the arrangements and restrictions may define relations between actors and/or properties of the actors
  - the resulting network may be multiple with different types of ties
- Then **data about the informal relations** between the actors have to be collected.
  - reactive data: surveys (friendship, flow of information, trust, assistance)
  - non-reactive data: email-contacts (like in the Enron case)

## A simple example

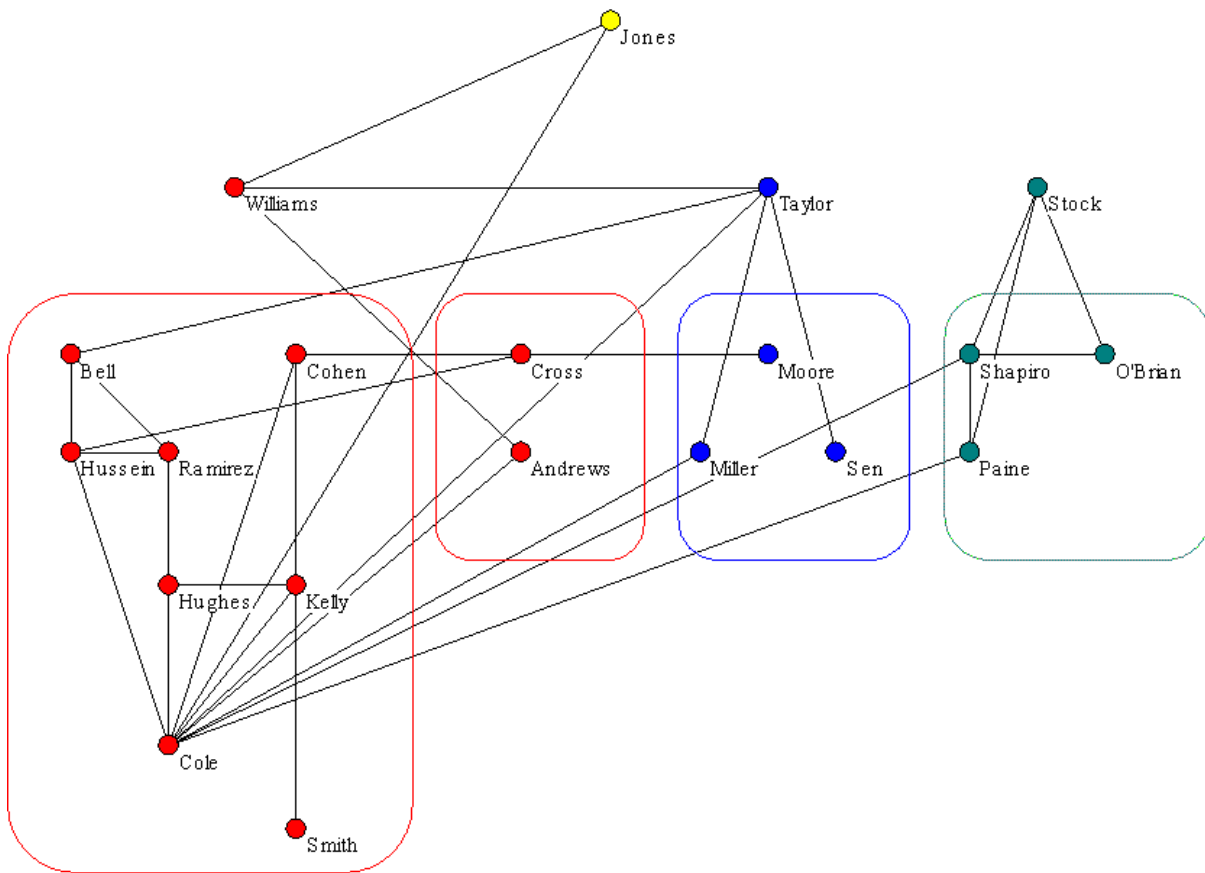


(<http://www.robcross.org/sna.htm>, Graphic: [http://www.robcross.org/images/sna\\_chart\\_01.gif](http://www.robcross.org/images/sna_chart_01.gif))

## Organizational model



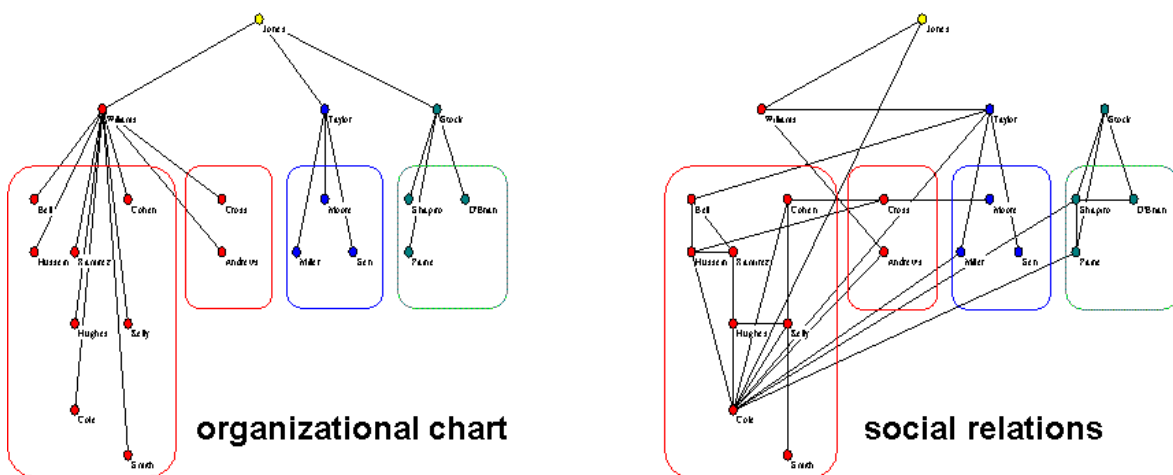
## Social relations



**Original question:**

"Please indicate the frequency with which you typically turn to each person below for information on work-related topics" : 0 - I don't know this person; 1 - never; 2 - seldom; 3 - sometimes; 4 - often; 5 - very often.

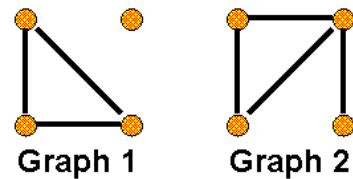
## How to compare these two graphs?



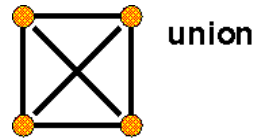
- Visually by coloring the conformities and the discrepancies.
- A set-theoretic notation proves to be helpful.

## Set-theoretic notation for graphs

We've got two undirected, unvalued graphs with the same node-set  $N$  and edge-sets  $E_1$  and  $E_2$ .



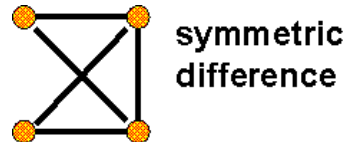
The **union** of these graphs is defined as graph with node-set  $N$  and edge-set  $E_{\text{Union}} = E_1 \cup E_2$ .



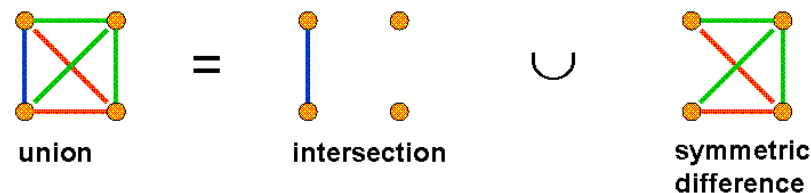
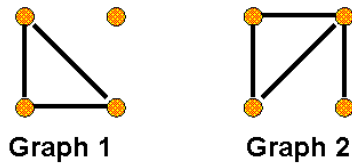
The **intersection** of these graphs is defined as graph with the node-set  $N$  and the edge-set  $E_{\text{Intersection}} = E_1 \cap E_2$ .



The **symmetric difference** of these graphs is defined analogously:  $E_{\text{sym.diff.}} = E_1 \Delta E_2$ .



## Comparing two graphs visually



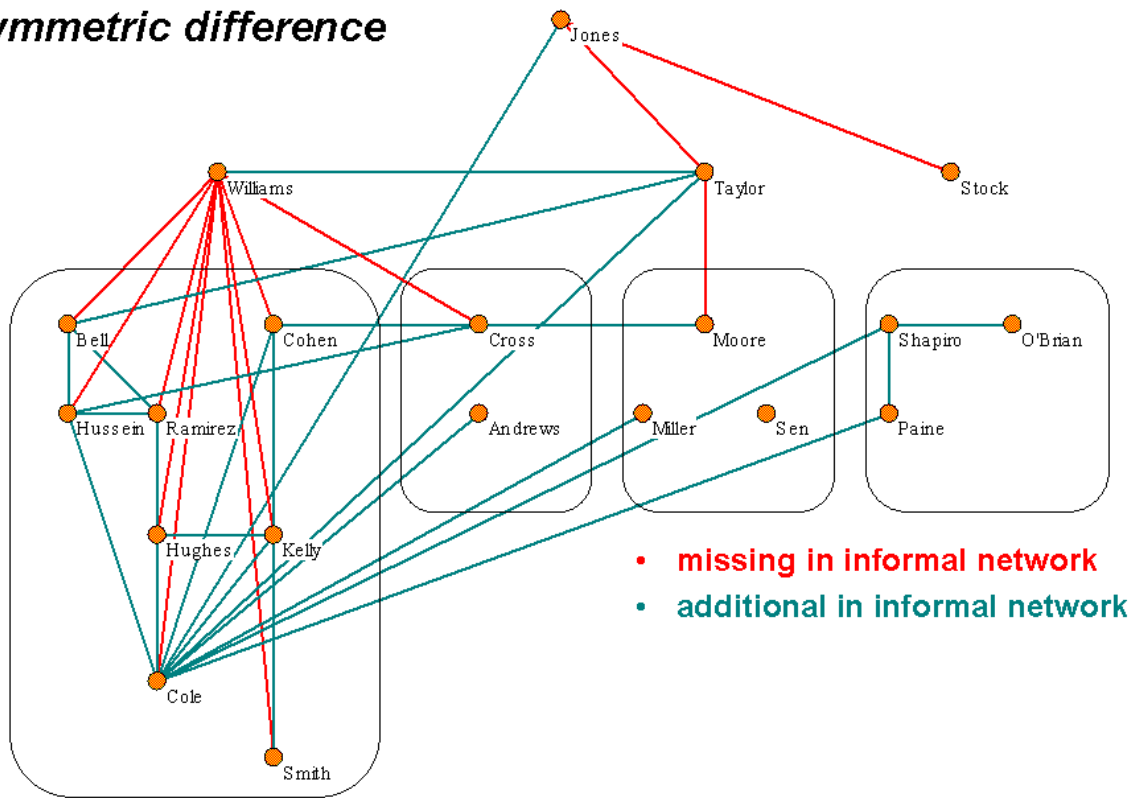
- blue edges:** belonging to both graphs
- red edges:** belonging to Graph1 but not to Graph2
- green edges:** belonging to Graph2 but not to Graph1

## Application of set-theoretic notation

- We take the Informal Network as starting point.
- The *symmetric difference* with the organizational model
  - on one hand defines those ties, which are “expected” by the organizational model but are in fact missing in the informal network (**deficit**)
  - on the other hand defines those ties, which are “not explained” by the organizational model but in fact present in the informal network (**surplus**)
- The intersection with the organizational model defines those ties in the Informal Network, which are “**explained**” by the organizational mode

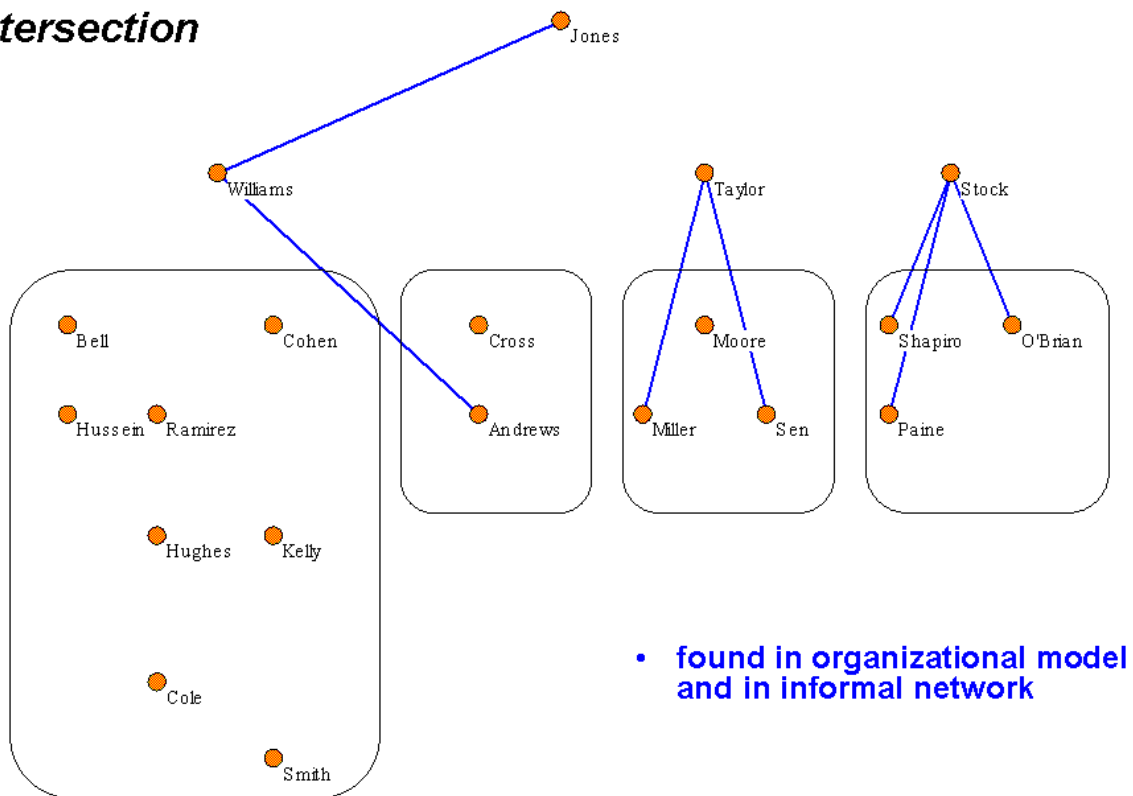
### Visualization 1: Discrepancies

#### *symmetric difference*



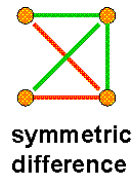
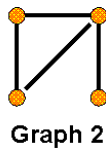
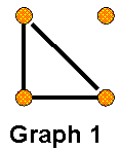
### Visualization 2: Conformities

#### *intersection*





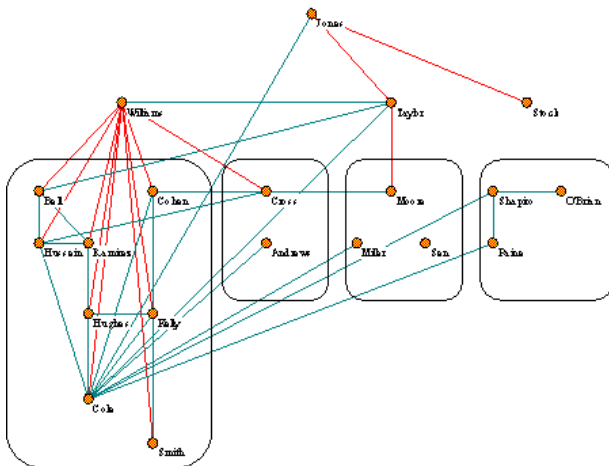
## Levenshtein-distance between graphs



- $L(\text{Graph1}, \text{Graph2}) = 5$  , because there are five discrepancies between Graph1 and Graph2 that have to be removed by the defined edit-operations to transform Graph1 into Graph2 or vice versa.
- This concept can be easily expanded to directed and to valued graphs over the same node-set.

## Application

The Levenshtein-distance between the organizational model and the informal network is given by the number of edges of the symmetric difference of these two networks.



symmetric difference:

- edges missing in informal network
- edges additional in informal network

For our example ( 20 nodes ) we find:  **$L = 36$**

(  $L_{\max} = \frac{1}{2} * 20 * 19 = 190$  ,  $L_r = 36/190 = 19\%$  )

## Discussion 2

- The analysis of an informal network in organization usual-ly is a stepwise or iterative process, during which different organizational models may be considered.
- Taken for itself the Levenshtein-distance is not very in-formative. But it allows us to compare the goodness of fit of the observed informal network to different organizational models.
- If the organizational model and the informal network are given as undirected, unvalued graphs with  $n$  nodes, the maximal Levenshtein-distance between two graphs is given as  $L_{\max} = \frac{1}{2} * n * (n-1)$  . This allows us to compare organizations of different size using the relative measure  $L_r = L / L_{\max}$  for each of it.

## Conclusion

- We outlined some ideas how to reveal the informal structure of organizations.
  - We showed how to visualize the discrepancies and conformities between organizational model and observed informal network
  - We gave a measure for the goodness of the fit of the observed informal network to an organizational model.
- Both concepts are easily extendable to directed (and valued) informal relations.
- There is a wide field of applications of the pro-posed concepts outside organizational research, e.g. the analysis of Cognitive Social Structure.

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