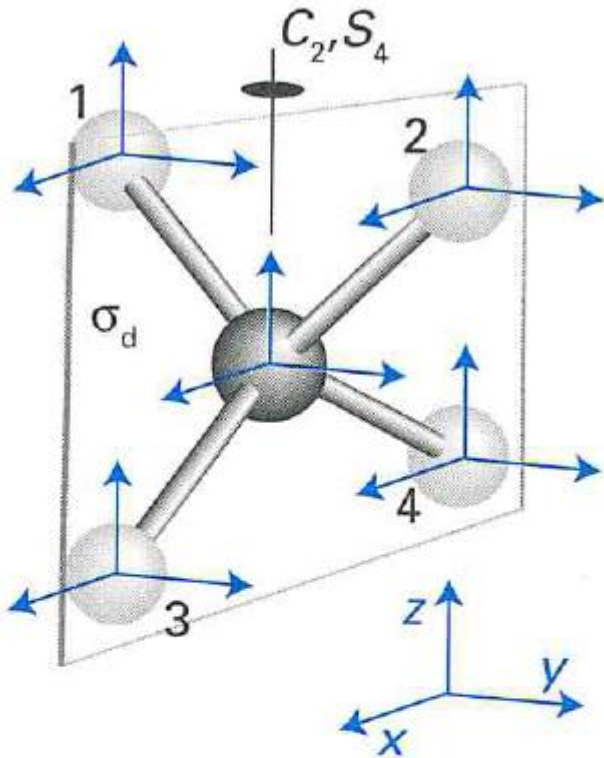


Schwingungsmoden von CH₄



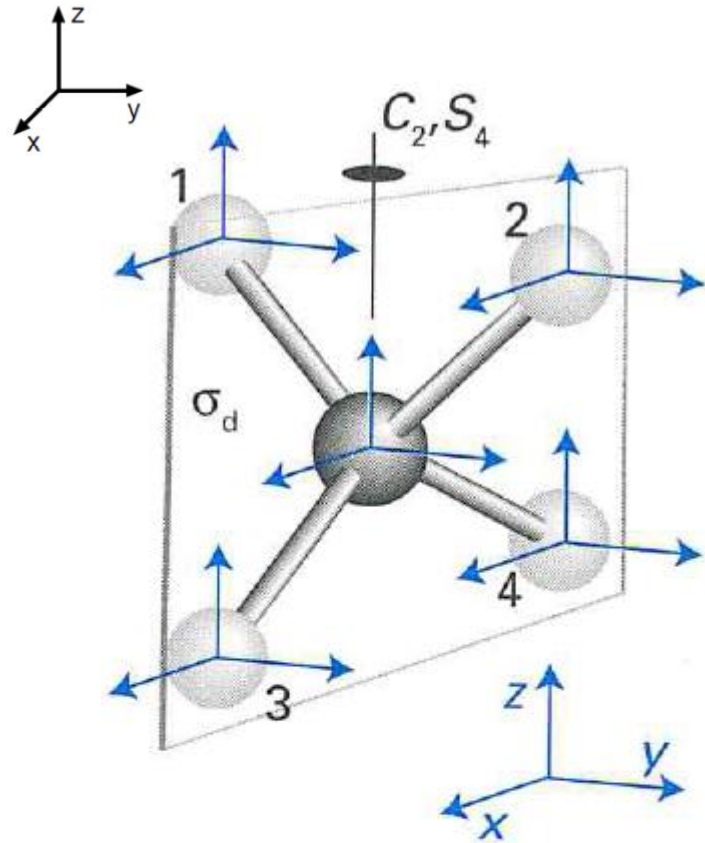
$T_d, \bar{4}3m$	E	$8C_3$	$3C_2$	$6\sigma_d$	$6S_4$	$h = 24$
A_1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1	
E	2	-1	2	0	0	$(3z^2 - r^2, x^2 - y^2)$
T_1	3	0	-1	-1	1	(R_x, R_y, R_z)
T_2	3	0	-1	1	-1	$(x, y, z), (xy, xz, yz)$

- 5 Symmetrieklassen
- 5 Symmetrierassen
- 24 Symmetrieoperationen (=h)

Fig. 10.27 The displacements used in the discussion of the normal modes of a tetrahedral methane molecule.

$S_4 =$ Molekülachse (damit auch C_2)
Bei Transformation (x,y,z) alle drei C_2 beachten!

Schwingungsmoden von CH₄



Charaktere der Symmetrieoperationen

$$\chi_E = 15$$

$$\chi_{C_2} = (-1 - 1 + 1) = -1$$

$$\chi_{\sigma_d} = (1 - 1 + 1) + (1 - 1 + 1) + (1 - 1 + 1) = 3$$

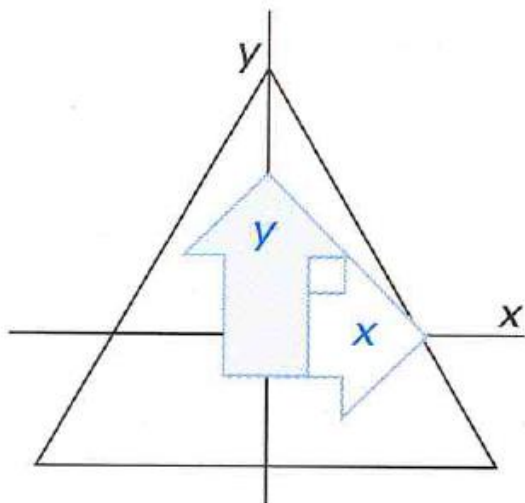
$$\chi_{S_4} = (0 + 0 - 1) = -1$$

$$\chi_{C_3} = ?$$

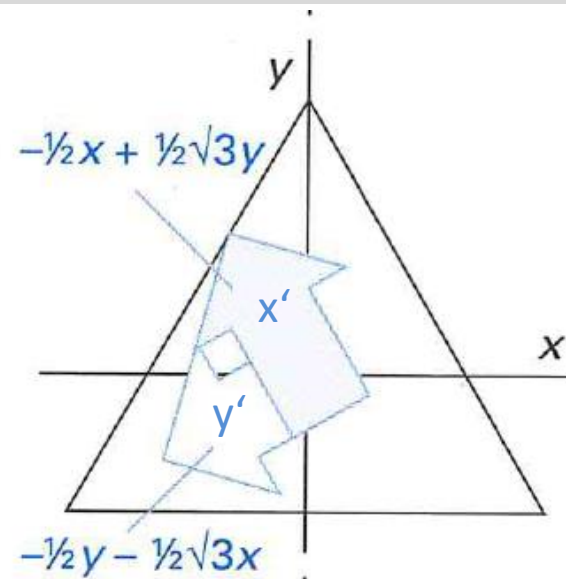
Fig. 10.27 The displacements used in the discussion of the normal modes of a tetrahedral methane molecule.

S_4 = Molekülachse (damit auch C_2)
Bei Transformation (x,y,z) alle drei C_2 beachten!

Zur Symmetrieoperation C_3



C_{3+}



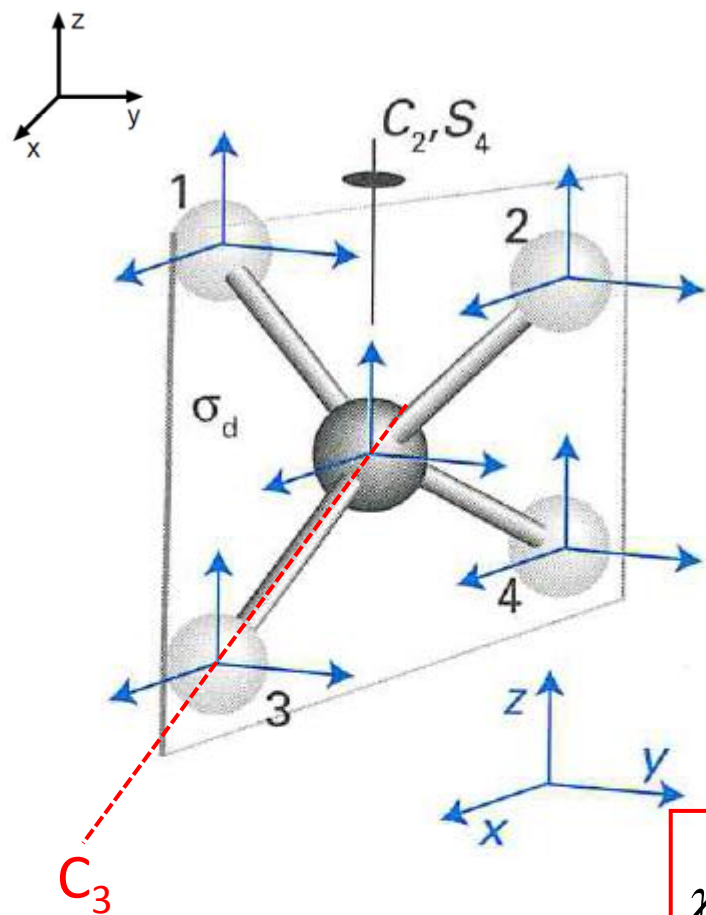
$$\vec{q}_x = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \vec{q}_y = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}, \vec{q}_z = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

$$\vec{q}_x' = \begin{pmatrix} -\cos(60^\circ) \\ +\sin(60^\circ) \\ 0 \end{pmatrix}, \vec{q}_y' = \begin{pmatrix} -\sin(60^\circ) \\ -\cos(60^\circ) \\ 0 \end{pmatrix}, \vec{q}_z' = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

$$\Gamma_{C_{3+}} = \begin{pmatrix} -1/2 & \sqrt{3}/2 & 0 \\ -\sqrt{3}/2 & -1/2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\chi_{C_{3+}} = 0$$

Schwingungsmoden von CH₄



Charaktere der Symmetrieeoperationen

$$\chi_E = (1+1+1) + (1+1+1) + (1+1+1) + (1+1+1) + (1+1+1) = 15$$

$$\chi_{C_2} = (-1-1+1) = -1$$

$$\chi_{\sigma_d} = (1-1+1) + (1-1+1) + (1-1+1) = 3$$

$$\chi_{S_4} = (0+0-1) = -1$$

$$\chi_{C_3} = \left(\left(-\frac{1}{2} \right) + \left(-\frac{1}{2} \right) + 1 \right) + \left(\left(-\frac{1}{2} \right) + \left(-\frac{1}{2} \right) + 1 \right) = 0$$

Fig. 10.27 The displacements used in the discussion of the normal modes of a tetrahedral methane molecule.

Reduzible Darstellung von CH₄

$$\Gamma_{ges} = c_1 A_1 + c_2 A_2 + c_3 E + c_4 T_1 + c_5 T_2$$

$$c_1(A_1) = \frac{1}{h} \sum_{i=1}^5 [n(R_i) \chi(R_i, A_1) \chi(R_i, CH_4)]$$

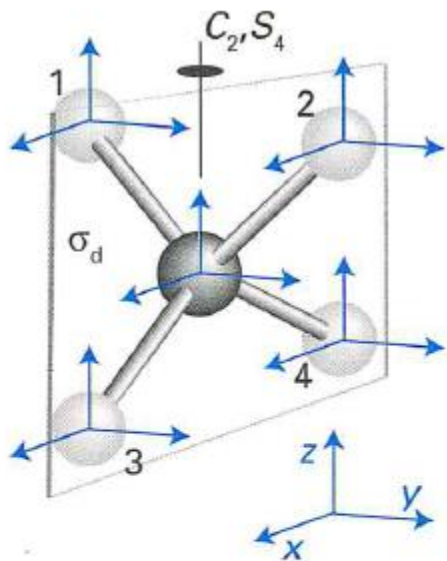
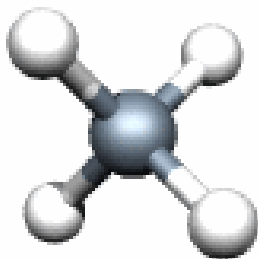


Fig. 10.27 The displacements used in the discussion of the normal modes of a tetrahedral methane molecule.

$T_d, \bar{4}3m$	E	$8C_3$	$3C_2$	$6\sigma_d$	$6S_4$	$h=24$
A_1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1	
E	2	-1	2	0	0	$(3z^2 - r^2, x^2 - y^2)$
T_1	3	0	-1	-1	1	(R_x, R_y, R_z)
T_2	3	0	-1	1	-1	$(x, y, z), (xy, xz, yz)$

	E	$8C_3$	$3C_2$	$6\sigma_d$	$6S_4$
$\chi_{R_i}(CH_4)$	15	0	-1	3	-1

Schwingungsmoden von CH₄



$T_d, \bar{4}3m$	E	$8C_3$	$3C_2$	$6\sigma_d$	$6S_4$	$h = 24$
A_1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1	
E	2	-1	2	0	0	$(3z^2 - r^2, x^2 - y^2)$
T_1	3	0	-1	-1	1	(R_x, R_y, R_z)
T_2	3	0	-1	1	-1	$(x, y, z), (xy, xz, yz)$

Reduzible Darstellung (3N x 3N Matrix):

$$\Gamma_{ges} = A_1 + E + T_1 + 3T_2 \quad (3N \text{ Freiheitsgrade})$$

Translation:

$$\Gamma_{trans} = T_2 \quad (3 \text{ FGs Translation})$$

Rotation:

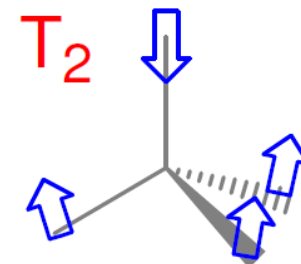
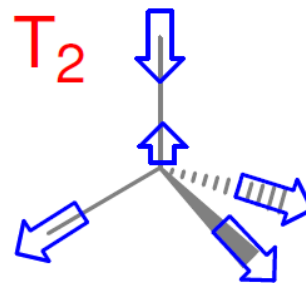
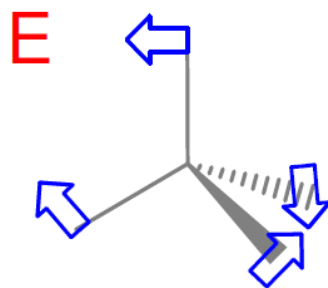
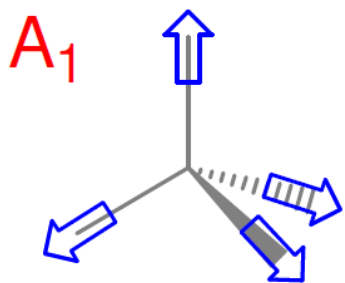
$$\Gamma_{rot} = T_1 \quad (3 \text{ FGs Rotation})$$

Schwingung:

$$\Gamma_{vib} = A_1 + E + 2T_2 \quad (3N-6 \text{ Schwingungen})$$

Schwingungsmoden von CH₄

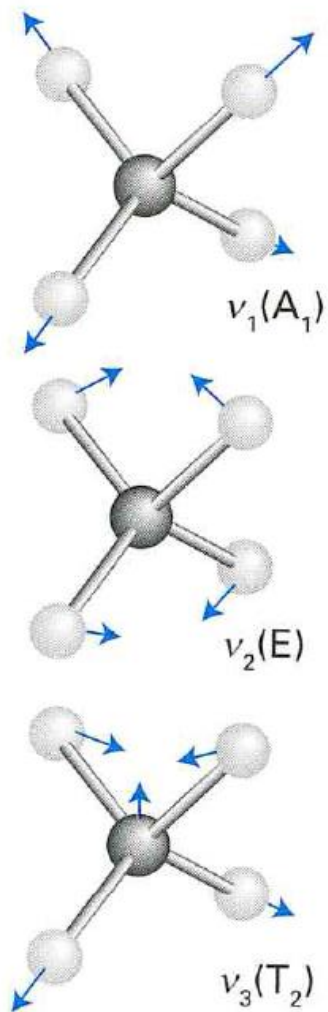
$$\Gamma_{vib} = A_1 + E + 2T_2$$



M. Hoffmann, Uni Heidelberg

$T_d, \bar{4}3m$	E	$8C_3$	$3C_2$	$6\sigma_d$	$6S_4$	$h=24$
A_1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1	
E	2	-1	2	0	0	$(3z^2 - r^2, x^2 - y^2)$
T_1	3	0	-1	-1	1	(R_x, R_y, R_z)
T_2	3	0	-1	1	-1	$(x, y, z), (xy, xz, yz)$

Schwingungsmoden von CH₄



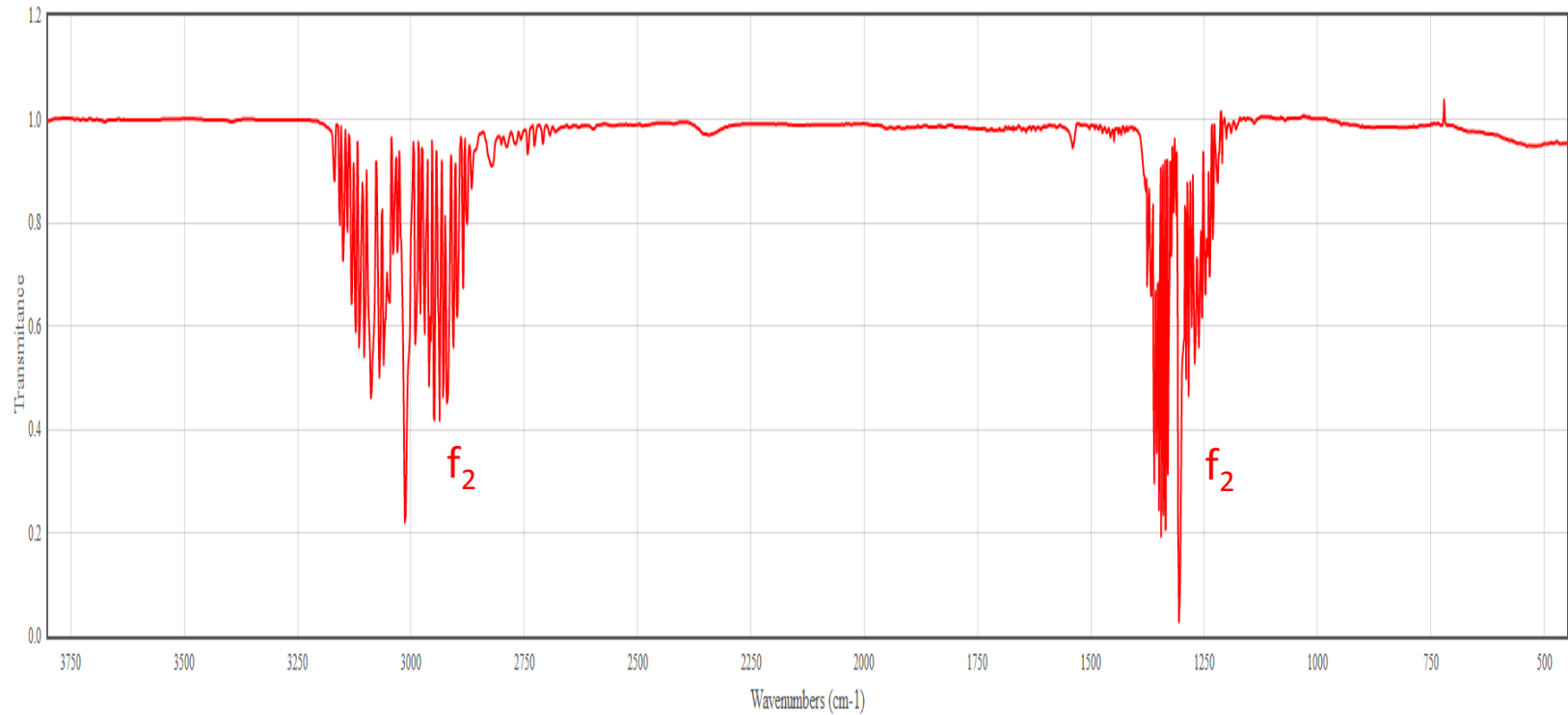
$T_d, \bar{4}3m$	E	$8C_3$	$3C_2$	$6\sigma_d$	$6S_4$	$h = 24$
A_1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1	
E	2	-1	2	0	0	$(3z^2 - r^2, x^2 - y^2)$
T_1	3	0	-1	-1	1	(R_x, R_y, R_z)
T_2	3	0	-1	1	-1	$(x, y, z), (xy, xz, yz)$

$$\Gamma_{vib} = \underbrace{A_1 + E + 2T_2}_{\text{green bracket}}$$

Fig. 10.28 Three representative normal modes of a tetrahedral molecule.

Schwingungsmoden von CH₄

Infrared Spectrum



a_1	1	Sym str	2917 cm ⁻¹
e	2	Deg deform	1534 cm ⁻¹
f_2	3	Deg str	3019 cm ⁻¹
f_2	4	Deg deform	1306 cm ⁻¹

Schwingungsmoden von SF₆

O _h (m3m)	E	8C ₃	6C ₂	6C ₂	3C ₂ (=C ₄ ²)	i	6S ₄	8S ₆	3σ _h	6σ _d	h=48	
A _{1g}	1	1	1	1	1	1	1	1	1	1		x ² +y ² +z ²
A _{2g}	1	1	-1	-1	1	1	-1	1	1	-1		
E _g	2	-1	0	0	2	2	0	-1	2	0		(2z ² -x ² -y ² , x ² -y ²)
T _{1g}	3	0	-1	1	-1	3	1	0	-1	-1	(R _x , R _y , R _z)	
T _{2g}	3	0	1	-1	-1	3	-1	0	-1	1		(xy, yz, xz)
A _{1u}	1	1	1	1	1	-1	-1	-1	-1	-1		
A _{2u}	1	1	-1	-1	1	-1	1	-1	-1	1		
E _u	2	-1	0	0	2	-2	0	1	-2	0		
T _{1u}	3	0	-1	1	-1	-3	-1	0	1	1	(x, y, z)	
T _{2u}	3	0	1	-1	-1	-3	1	0	1	-1		

Reduzible Darstellung (3N x 3N Matrix):

$$\Gamma_{ges} = A_{1g} + E_g + T_{1g} + T_{2g} + 3T_{1u} + T_{2u} \quad (3N \text{ Freiheitsgrade})$$

Translation: $\Gamma_{trans} = T_{1u} \quad (3 \text{ FGs Translation})$

Rotation: $\Gamma_{rot} = T_{1g} \quad (3 \text{ FGs Rotation})$

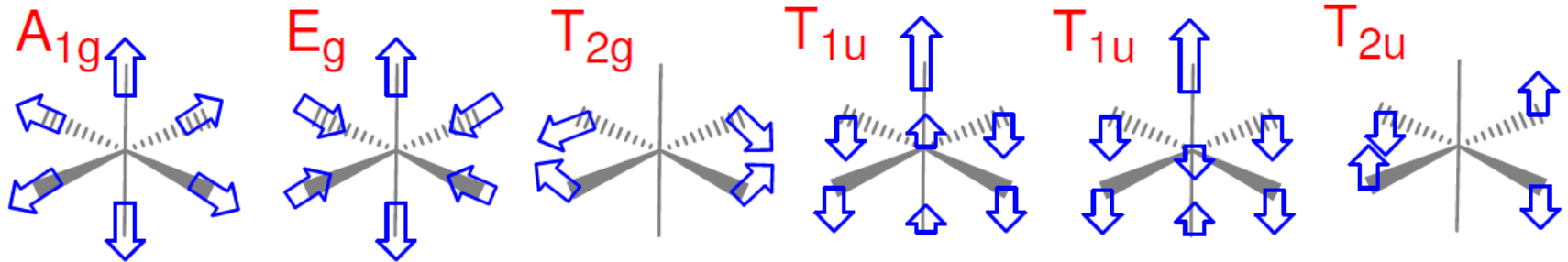
Schwingung: $\Gamma_{vib} = A_{1g} + E_g + 2T_{1u} + T_{2g} + T_{2u} \quad (3N-6 \text{ Schwingungen})$



Schwingungsmoden von SF₆

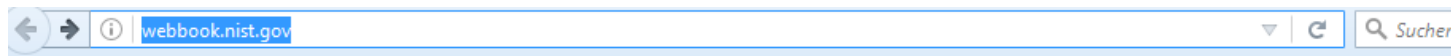
O _h (m3m)	E	8C ₃	6C ₂	6C ₂	3C ₂ (=C ₄ ²)	i	6S ₄	8S ₆	3σ _h	6σ _d	h=48	
A _{1g}	1	1	1	1	1	1	1	1	1	1		x ² +y ² +z ²
A _{2g}	1	1	-1	-1	1	1	-1	1	1	-1		
E _g	2	-1	0	0	2	2	0	-1	2	0		(2z ² -x ² -y ² , x ² -y ²)
T _{1g}	3	0	-1	1	-1	3	1	0	-1	-1	(R _x , R _y , R _z)	
T _{2g}	3	0	1	-1	-1	3	-1	0	-1	1		(xy, yz, xz)
A _{1u}	1	1	1	1	1	-1	-1	-1	-1	-1		
A _{2u}	1	1	-1	-1	1	-1	1	-1	-1	1		
E _u	2	-1	0	0	2	-2	0	1	-2	0		
T _{1u}	3	0	-1	1	-1	-3	-1	0	1	1	(x, y, z)	
T _{2u}	3	0	1	-1	-1	-3	1	0	1	-1		

$$\Gamma_{vib} = A_{1g} + E_g + 2T_{1u} + T_{2g} + T_{2u}$$



Online Datenbank zu IR-Spektren

<http://webbook.nist.gov>



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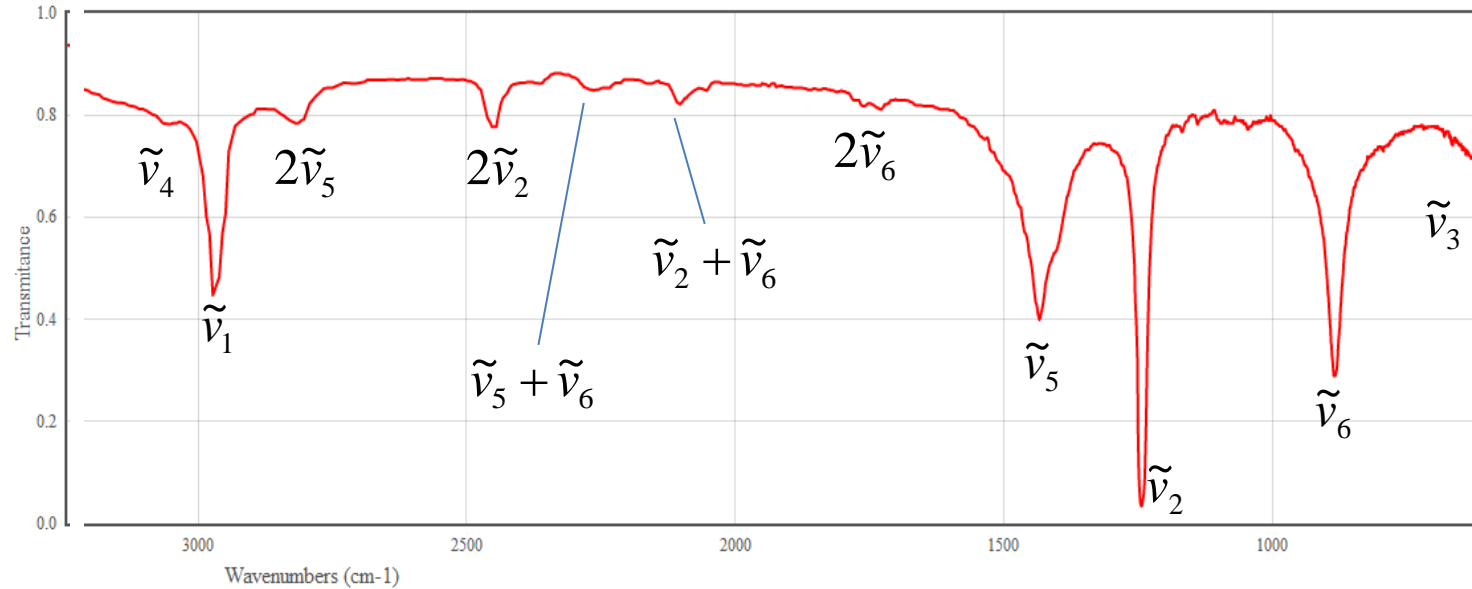
The NIST Chemistry WebBook provides access to data compiled and distributed by NIST under the [Standard Reference Data Program](#).

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 - Enthalpy of formation
 - Enthalpy of combustion
 - Heat capacity
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- **Electronic and vibrational spectra for over 5000 compounds.**
- **Constants of diatomic molecules (spectroscopic data) for over 600 compounds.**

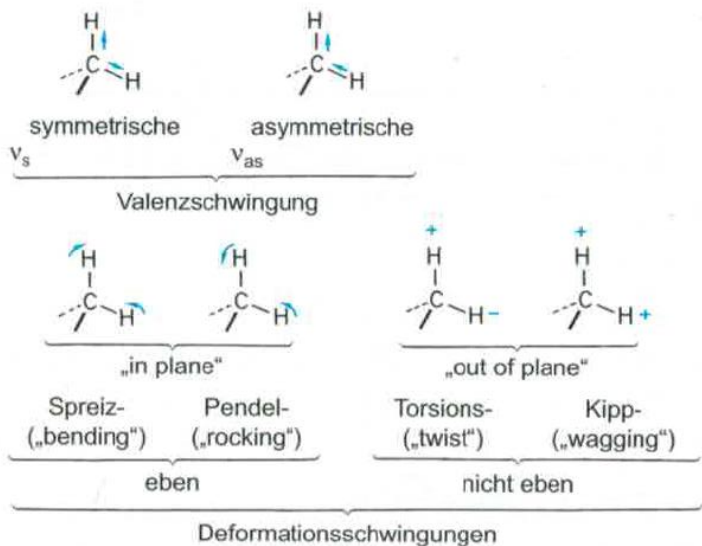
Schwingungen mehratomiger Moleküle: CH₃I

<http://webbook.nist.gov/cgi/cbook.cgi?ID=C74884&Mask=80>



$$A_1 \left\{ \begin{array}{l} \tilde{\nu}_1 = 2970 \text{ cm}^{-1} \\ \tilde{\nu}_2 = 1252 \text{ cm}^{-1} \\ \tilde{\nu}_3 = 533 \text{ cm}^{-1} \end{array} \right. \quad \left. \begin{array}{l} \tilde{\nu}_4 = 3060 \text{ cm}^{-1} \\ \tilde{\nu}_5 = 1440 \text{ cm}^{-1} \\ \tilde{\nu}_6 = 880 \text{ cm}^{-1} \end{array} \right\} E$$

Gruppenschwingungen im IR



+ = Schwingung vor der Papierebene
 - = Schwingung hinter der Papierebene

Table 6.3 Typical bond-stretching and angle-bending group vibration wavenumbers $\tilde{\nu}$.

Bond-stretching		Bond-stretching	
Group	$\tilde{\nu}/\text{cm}^{-1}$	Group	$\tilde{\nu}/\text{cm}^{-1}$
$\equiv\text{C}-\text{H}$	3300	$-\text{O}-\text{H}$	3600‡
$=\text{C}-\text{H}$	3020	$>\text{N}-\text{H}$	3350
except $\text{O}=\text{C}-\text{H}$	2800	$\equiv\text{P}=\text{O}$	1295
$\equiv\text{C}-\text{H}$	2960	$>\text{S}=\text{O}$	1310
$-\text{C}\equiv\text{C}-$	2050	Angle-bending	
$>\text{C}=\text{C}<$	1650	$\equiv\text{C}-\text{H}$	700
$\equiv\text{C}-\text{C}<$	900	$=\text{C}-\text{H}$	1100
$>\text{Si}-\text{Si}<$	430	$-\text{C}-\text{H}$	1000
$>\text{C}=\text{O}$	1700	$-\text{C}-\text{H}$	1450
$-\text{C}\equiv\text{N}$	2100	$\text{C}\equiv\text{C}-\text{C}$	300
$\equiv\text{C}-\text{F}$	1100		
$\equiv\text{C}-\text{Cl}$	650		
$\equiv\text{C}-\text{Br}$	560		
$\equiv\text{C}-\text{I}$	500		

Symmetrie von Gruppenschwingungen

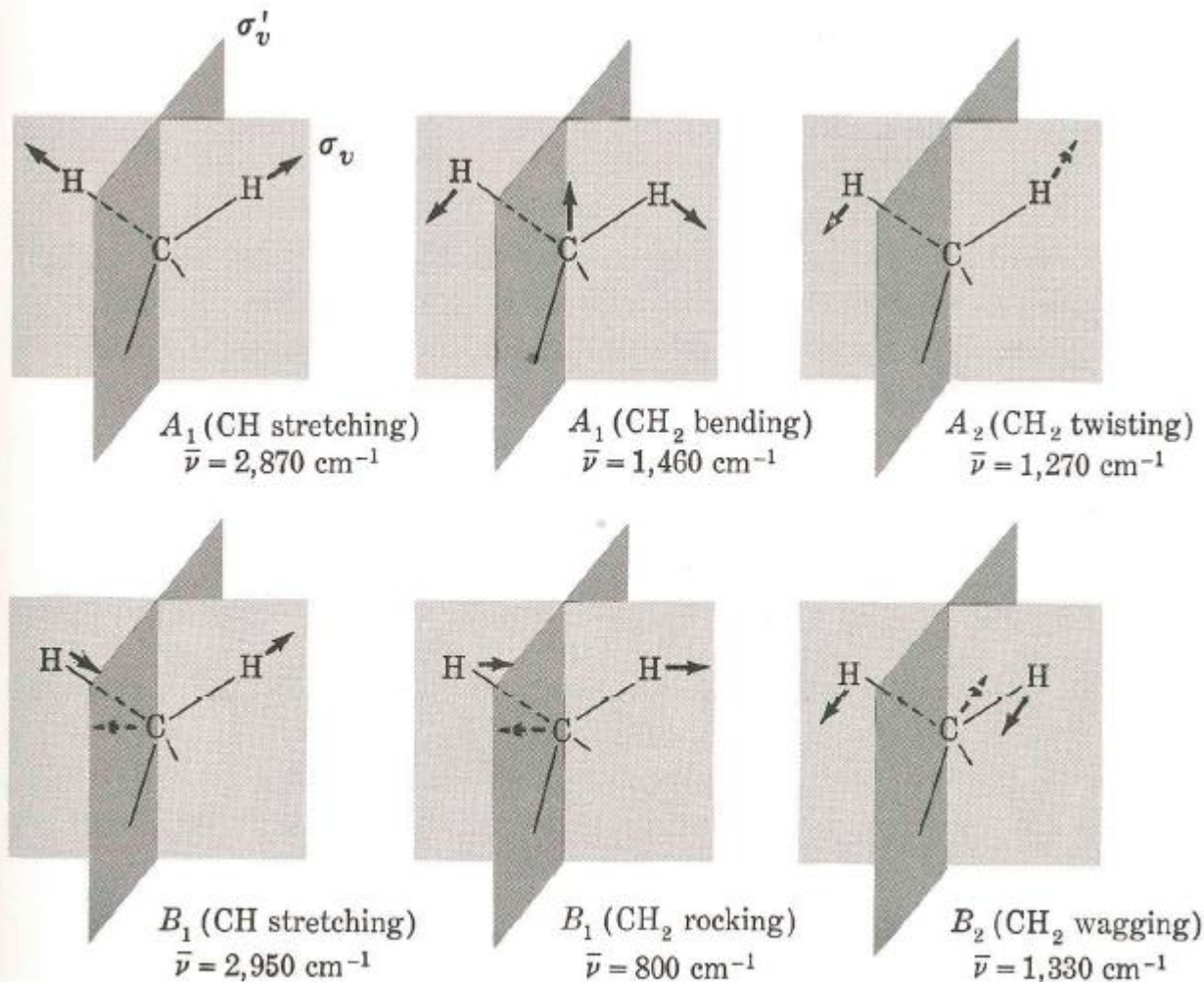


Fig. 8-21 Various vibrational modes of the methylene group. (By permission of G. M. Barrow, "Introduction to Molecular Spectroscopy," McGraw-Hill Book Company, New York, 1962.)